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## INCLUDING OF ADMIXTURE BORON ATOMS IN THE ELECTRIC NONACTIVE STATE TO SILICON SINGLE-CRYSTAL

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According of to experimental data by means of mathematical modeling was evaluated the proportion of those nonactive boron atoms, which are part of a single crystal silicon in an electrically inactive state at various stages of his growing by the of Czochralskij method. Keywords: silicon, single crystal, boron, nonactive, electrically inactive impurity

*Introduction*. The single-crystals of silicon for providing of p-type for conductivity alloy by an acceptor impurity, mostly - by boron. However part of atoms of boron in a crystal can enter in the complement of various microflaws and complexes [1]. Such atoms do not form covalently connections with the atoms of silicon and can not form a hole, id est, there are electric nonactive

The size of concentration and state of alloying admixture determine one of major factors of quality of silicon single-crystals - its specific electric resistance. A control by the concentration of all admixtures in the given limits is an actual task at the production of silicon single-crystals for microelectronics and sun energy.

State of question. The concentration of admixture in a single-crystal which is grown from fusion depends on the effective coefficient of distribution of this admixture between the liquid and hard phases k [2]:

$$k = \frac{N_{ms}}{N_p} \cdot \frac{\gamma_p}{\gamma_{ms}} \,, \tag{1}$$

where  $N_{ms}$ ,  $N_p$  are a concentration of admixture atoms accordingly in hard and liquid phases, at/sm<sup>3</sup>;  $\gamma_p$ ,  $\gamma_{ms}$  are a density of these phases, tr/m<sup>3</sup>.

Effective coefficient for distribution of most admixtures in silicon less than one (for boron  $0.8 \le k \le 1.0$ ) [3] as a result of their partial pushing away from front of crystallization in fusion. Therefore in the process of drawing out of single-crystal in fusion by Czochralskij method there is a gradual accumulation of boron admixture in fusion, thus its concentration in the grown single-crystal increases gradually. Distribution of admixture in fusion and single-crystal for the tend of crystallization it is possible to characterize analytical expressions which are based on V. Pfann works [4]:

$$N_{p}(g) = N_{0}(1-g)^{k-1}, (2)$$

$$N_{me}(g) = \frac{\gamma_{me}}{\gamma_p} \cdot k \cdot N_0 \cdot (1 - g)^{k-1}, \qquad (3)$$

where  $N_0$  is an initial concentration of admixture atoms n a liquid phase (to beginning of crystallization), at/sm<sup>3</sup>; g is part of initial mass of fusion, which passed to the hard phase in the moment of crystallization of portion crystal with the concentration of admixture of  $N_{ms}(g)$ , at/sm<sup>3</sup>

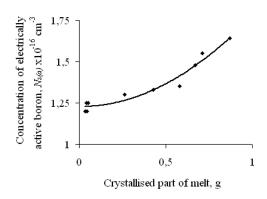
In work [2] it was shown by a mathematical analysis, that a function  $N_{mB}(g)$  from equation (3) is ambiguous, and the physical admissions used for its conclusion executed not on all stages of process of grow after Czochralskij method. In this work a new model was worked out for dependence  $N_{mg}(g)$ , which is based on equation of balance of atoms of not volatile admixture of boron during all process of drawing out from fusion of single-crystal by Czochralskij method. With use of this model the effective coefficient of distribution k is determined on experimental dependence  $N_{mg}(g)$ :

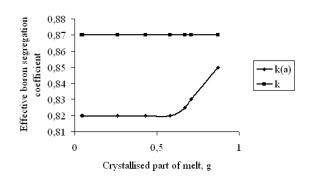
$$k(g) = \frac{(1-g) \cdot N_{ms}(g)}{\frac{\gamma_{ms}}{\gamma_{ns}} \cdot N_0 - \int_0^g N_{ms}(g) dg} . \tag{4}$$

On the same principle there were the worked out models of  $N_{ms}(g)$  and k(g) for the carbon and oxygen admixtures [5]. In Czochralskij method speed of crystallization V on the finishing stage of growing is diminished on technological reasons. From the kinetic theory of crystallization from fusion follows, that with diminishing V the effective coefficient of distribution for any admixture k must also diminish. In this work it was shown that in an experiment the coefficients of admixtures for carbon  $k_C$  and oxygen  $k_O$  diminish with diminishing V of single-crystal of silicon, alloying by far stronger than it is forecast by the kinetic theory of crystallization. At the same time the size of effective coefficient of distribution for boron k with diminishing of speed of single-crystal growing from fusion instead of diminishing grows. At fact of considerable difference of experimental dependences k(g) admixtures in silicon from speed of height from theoretical in work [6] admission was done, that during growing by Czochralskij method the processes of complexaction change in the single-crystal silicon as a result of change correlation of concentrations for all admixtures.

*Problem formulation.* Task of this research is estimation on experimental data in the single-crystals silicon part of atoms of alloying admixture of boron, which are electric nonactive as a result of included in composition of complexes and microflaws.

Basic part of researches. Seven single-crystals silicon of brand KGB 0.5-1.7/10 with diameter a 135 mm and a crystallography orientation {100} are investigated. Crystals were grown by Czochralskij method at industrial conditions in setting as "Redmet-30" from identical raw material. A concentration electric active atoms of alloying admixture of boron was calculated on the size of specific electric resistance, that measured by four-prove method [7,8]. The experimental results of concentration electric active atoms of boron  $N_{ms}(g)$  generalized on seven single-crystals are offered to fig. 1, and calculated for to data  $N_{ms}(g)$  dependence of effective coefficient of distribution electric active atoms of boron k(a) - on fig. 2. Accepting that the looked increase of size k(a) on the late stages of growing is related to diminishing of part electric nonactive atoms of boron in single-crystals. For determination of effective coefficient distribution for all atoms of boron k (electric active and nonactive) will consider their distribution between liquid and hard phases at the beginning of single-crystal growing.





**Figure 1** is distribution electric active atoms of cron in single-crystals silicon

**Figure 2** is the effective coefficient of distribute boron: k(a) - electric active atoms; k - genera

As industrial conditions measure the concentration of admixtures in fusion  $N_p$  is impossible, we determine its on data of measuring  $N_{ms}(g)$  on a formula (1)

$$N_{p}(g) = \frac{N_{me(a)}(g)}{k_{(a)}} \cdot \frac{\gamma_{p}}{\gamma_{me}}.$$
 (5)

On the graphic fig. 1 and fig. 2 by approximations determine  $N_{mg}(0.01)$  and k(0,01), id est. in the overhead crossing of single-crystal, when g = 0.01.

From formula (5) find the concentration of boron atoms in fusion  $N_p(0.01)$ . The complete concentration of boron in initial fusion  $N_0$  we determine on its concentration in raw material:

$$N_0 = N_{cup} \cdot \frac{\gamma_p}{\gamma_{mg}} = 1,45 \cdot 10^{16} \cdot \frac{2,53}{2,33} = 1,574 \cdot 10^{16} \text{ sm}^{-3}.$$

Farther from formula (2) find the value of effective coefficient of distribution for all atoms of boron k (together electric active and nonactive).

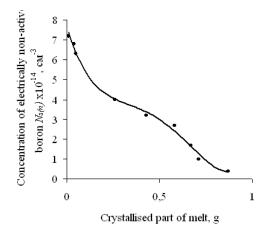
Where:

$$k = 1 + \frac{\log \frac{N_p(0,01)}{N_0}}{\log 0.99} . ag{6}$$

After the substitution of data g = 0.01;  $N_{TB}(0.01) = 1.19 \cdot 10^{16}$  sm<sup>-3</sup>; k(0.01) = 0.82;  $\gamma_p = 2.53$  t/m<sup>3</sup> and  $\gamma_{mg} = 2.33$  t/m<sup>3</sup> we find: k = 0.87. Now from formula (1) it is possible to find dependence of concentration electric nonactive atoms of boron  $N_{mg(H)}$  in a single-crystal on the different stages of its growing:

$$k(g) = \frac{N_{me(a)}(g) + N_{me(n)}(g)}{N_p(g)} \cdot \frac{\gamma_p}{\gamma_{me}}, \qquad (7)$$

where 
$$N_{ms(n)}(g) = \frac{\gamma_{ms}}{\gamma_p} \cdot k(g) \cdot N_0 \cdot (1-g)^{k-1} - N_{ms(a)}(g)$$
.



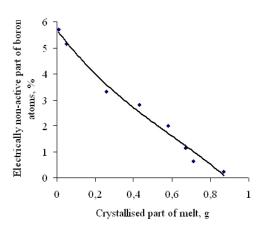


Figure 3 is concentration electric of nonactive Figure 4 is relative concentration electric of atoms to boron in the single-crystals of silicon

atoms of boron in the single-crystals of silicon

We accept, that k(g) = const, as it was accepted in work [4], id est. k(g) = const0.87 (fig. 2). Using experimental data  $N_{ms}(g)$  from fig. 1, expect dependence  $N_{ms}$ fig. 3) and  $N_{me}(g)/N_{me}$  (fig. 4). From data of fig. 4 it is evidently that during growing of single-crystal part electric nonactive atoms of boron in its diminishes substantially.

Conclusions. From estimations, got from experimental data by a mathematical modeling, follows, that part of alloying admixture boron, which is in the singlecrystal silicon in electric nonactive state, diminishes during the process of crystallization. The most credible reason of such phenomenon it is possible to consider diminishing of formation of complexes boron-oxygen as a result of the gradual diminishing of concentration of admixture of oxygen in the single-crystal of silicon from overheard to its underbody during growing on Czochralskij method.

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